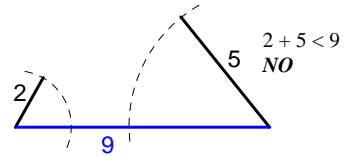
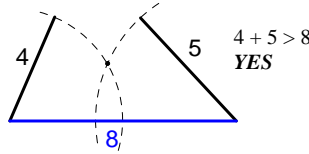


Geometry SOL Practice

Topic #7: Triangle Inequalities

Notes

I. Given 3 segment lengths, will they make a triangle?



Generalization

Given: short side, middle side, long side
 If short side + middle side > long side
 then **YES** a triangle can be form. Otherwise, **NO**.

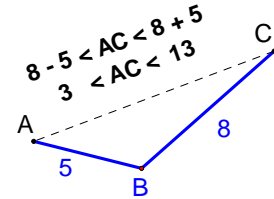
Example

Given:
 side 1 = 8 inches
 side 2 = 10 inches
 side 3 = 7 inches
 Is $8 + 7 > 10$?
 Is $15 > 10$? → **YES**

Example

Given:
 side 1 = 16 inches
 side 2 = 5 inches
 side 3 = 9 inches
 Is $5 + 9 > 16$?
 Is $14 > 16$? → **NO**

II. Given 2 sides of a triangle, what is the range of the third side?



Generalization

Given: **side 1** and **side 2**
 $|\text{side 1} - \text{side 2}| < \text{side 3} < \text{side 1} + \text{side 2}$
 or
subtract the sides < side 3 < add the sides

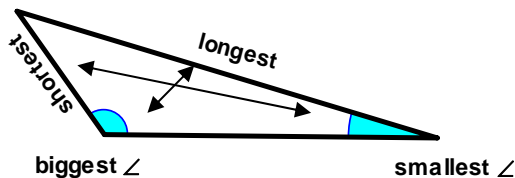
Example

Given:
 side 1 = 11 inches
 side 2 = 15 inches
 $15 - 11 < \text{side 3} < 15 + 11$
 $4 < \text{side 3} < 26$
 [Side 3 is between 4 and 26 inches.]

III. Given the sides of a triangle, list the angles in order of size.
 Given the angles of a triangle, list the sides in order of size.

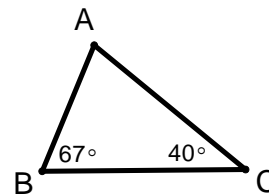
Generalization

The smallest angle is opposite the shortest side.
 The largest angle is opposite the longest side.



Example

Given: $m\angle B = 67^\circ$ and $m\angle C = 40^\circ$
 List the sides in order from shortest to longest.
 [note: $m\angle A = 180^\circ - 67^\circ - 40^\circ = 73^\circ$]



solution: **AB < AC < BC**