

## Study Guide

**Writing Linear Equations in Slope-Intercept Form**

The  $x$ -coordinate of the point where a line crosses the  $x$ -axis is called the  **$x$ -intercept**. Similarly, the  $y$ -coordinate of the point where the line crosses the  $y$ -axis is called the  **$y$ -intercept**.

**Slope-Intercept Form of a Linear Equation**

Given the slope  $m$  and the  $y$ -intercept  $b$  of a line, the slope-intercept form of an equation of the line is

$$y = mx + b.$$

If an equation is given in standard form  $Ax + By = C$  and  $B$  is not zero, the slope of the line is  $-\frac{A}{B}$  and the  $y$ -intercept is  $\frac{C}{B}$ .

The  $x$ -intercept is  $\frac{C}{A}$  where  $A \neq 0$ .

**Example:** Find the  $x$ - and  $y$ -intercepts of the graph of  $5x - 2y = 10$ . Then write the equation in slope-intercept form.

Since  $A = 5$ ,  $B = -2$ , and  $C = 10$ ,

$$\begin{aligned} \frac{C}{A} &= \frac{10}{5} & \frac{C}{B} &= \frac{10}{-2} & m &= -\frac{A}{B} \\ &= 2 & &= -5 & &= \frac{5}{2} \end{aligned}$$

Thus, the  $x$ -intercept is 2, and the  $y$ -intercept is  $-5$ . The equation of the line in slope-intercept form is

$$y = \frac{5}{2}x - 5.$$

**Find the  $x$ - and  $y$ -intercepts of the graph of each equation.**

1.  $5x + 4y = 20$

2.  $2x - 5y = -7$

3.  $4x - 8y = 10$

4.  $9x + y = -1$

**Write an equation in slope-intercept form of a line with the given slope and  $y$ -intercept. Then write the equation in standard form.**

5.  $m = 6, b = 10$

6.  $m = 4, b = 0$

7.  $m = -1, b = 3$

8.  $m = 2, b = -3$

**Find the slope and  $y$ -intercept of the graph of each equation. Then write each equation in slope-intercept form.**

9.  $0.2x + 0.5y = 1.6$

10.  $3x + 7y = 10$

11.  $6x - y = 9$

12.  $14x - 21y = 7$