

## Study Guide

## Functions

A special type of relation is called a **function**.

## Definition of Function

A **function** is a relation in which each element of the domain is paired with *exactly* one element of the range.

**Example 1:** Is  $\{(6, -3), (4, 1), (7, -2), (-3, 1)\}$  a function? Is the inverse a function?

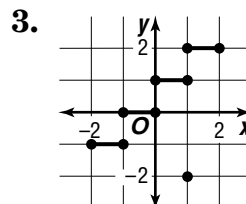
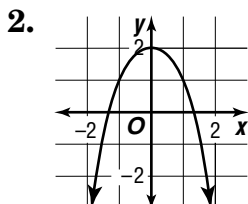
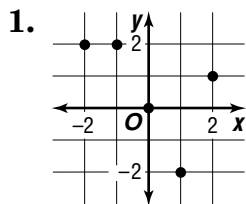
Since each element of the domain is paired with exactly one element of the range, the relation *is* a function. The inverse is not a function because 1 is paired with more than one element of the range.

The equation  $y = 2x + 1$  can be written as  $f(x) = 2x + 1$ . If  $x = 3$ , then  $f(3) = 2(3) + 1$ , or 7. Thus,  $f(3)$ , which is read “ $f$  of 3” is a way of referring to the value of  $y$  that corresponds to  $x = 3$ .

**Example:** If  $f(x) = 3x - 4$ , find  $f(3)$  and  $f(-2)$ .

$$\begin{aligned} f(3) &= 3(3) - 4 & f(-2) &= 3(-2) - 4 \\ &= 9 - 4 & &= -6 - 4 \\ &= 5 & &= -10 \end{aligned}$$

**Determine whether each relation is a function.**



4.  $\{(4, 2), (2, 3), (6, 1)\}$

5.  $\{(-3, -3), (-3, 4), (-2, 4)\}$

6.  $\{(-1, 0), (1, 0)\}$

7.  $-2x + 4y = 0$

8.  $x^2 + y^2 = 8$

9.  $-\frac{1}{4}x = -\frac{1}{4}y - 2$

**Given  $f(x) = 2x - 4$  and  $g(x) = x^2 - 4x$ , find each value.**

10.  $f(4)$

11.  $g(2)$

12.  $f(-5)$

13.  $g(-3)$

14.  $f\left(\frac{1}{4}\right)$

15.  $g\left(\frac{1}{4}\right)$